



# Structural Analysis & Design Software

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Webinar

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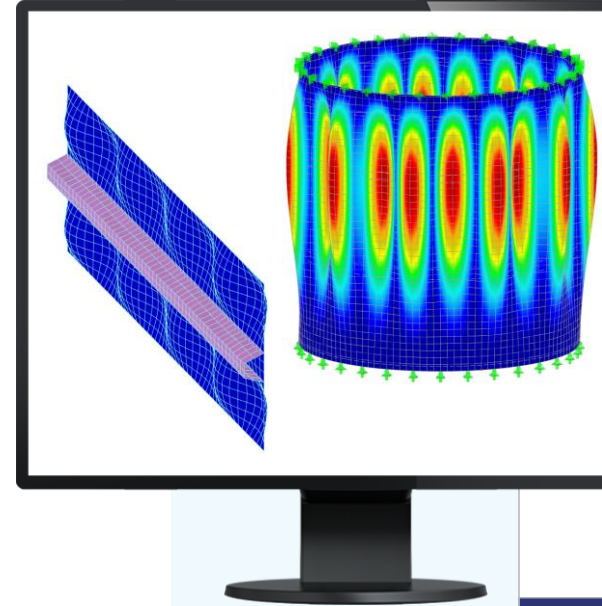
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# Plate and Shell Buckling Utilizing Dlubal Software



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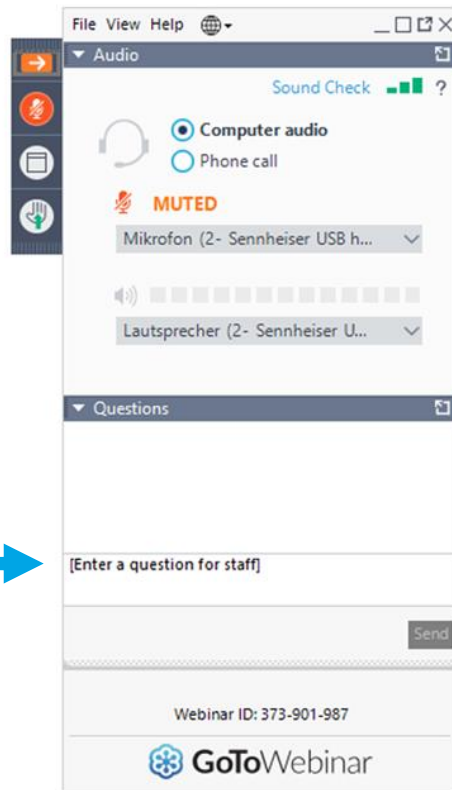


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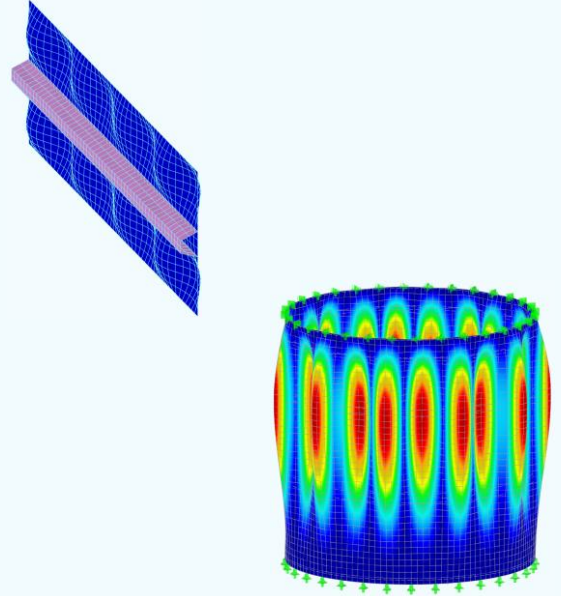
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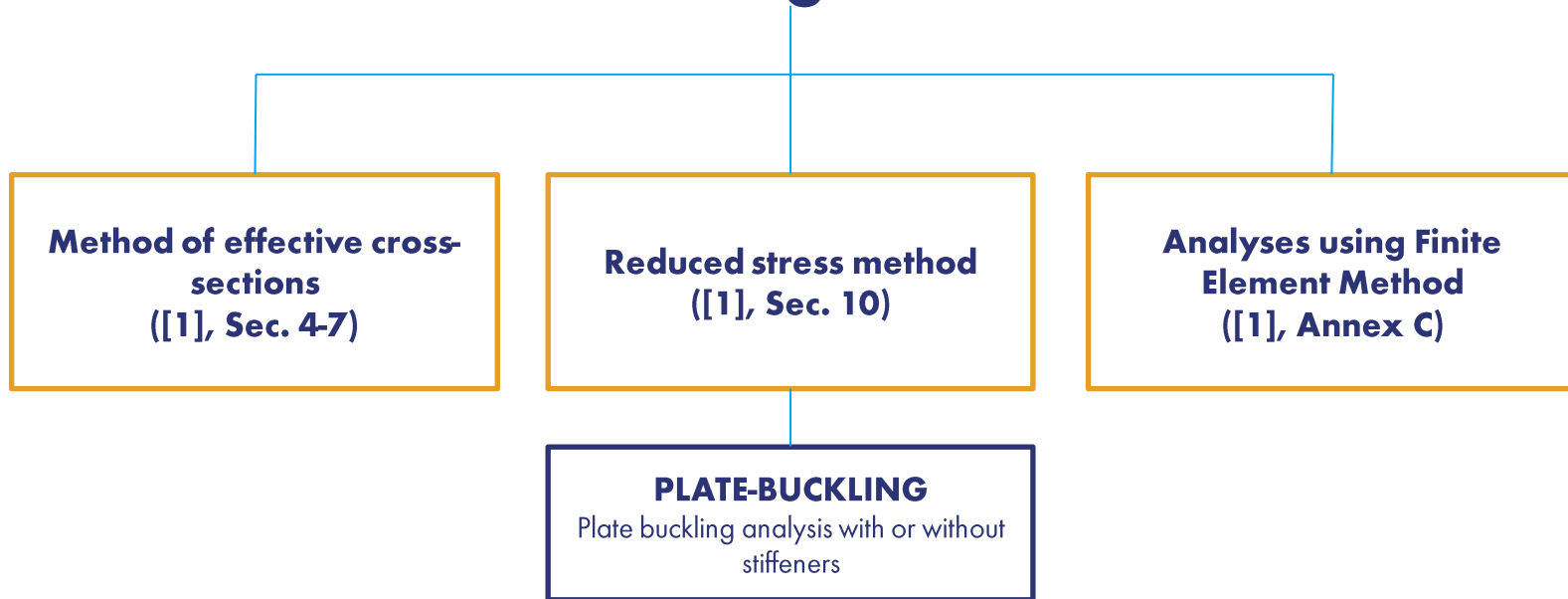
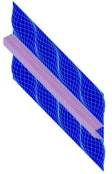
# CONTENT

- 01 Plate buckling design according to EN 1993-1-5 in PLATE-BUCKLING
- 02 Shell buckling design utilizing the global MNA and LBA calculation according to EN 1993-1-6 with RFEM



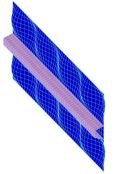


# Plate Buckling Analyses of Steel Plates According to EN1993-1-5





# Example: Buckling Analysis of a Stiffened Plate with PLATE-BUCKLING (Reduced Stress Method)



## Data

Material: S 355

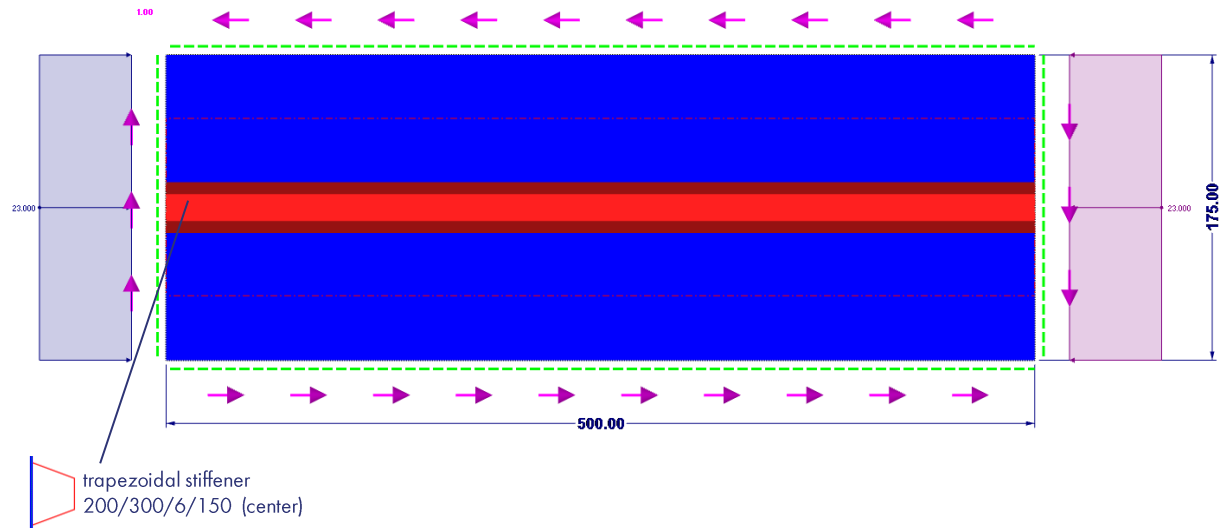
Plate thickness:  $t = 14 \text{ mm}$

## Stresses

$$\sigma_1 = \sigma_2 = 23.0 \text{ kN/cm}^2$$

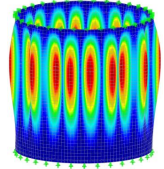
$$\tau = 1.0 \text{ kN/cm}^2$$

## System





# Plate Buckling Analyses of Steel Shell Structures acc. to EN1993-1-6



## Stress-based plate buckling analysis

- Simple application for expert engineers
- Low requirements for computer technology (often hand calculation formulas used)
- Economic results difficult to achieve for load situations significantly differing from conventional buckling shapes

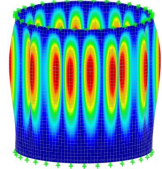
## Plate buckling design by global numerical MNA/LBA analysis

- More background knowledge for shell stability required
- Higher requirements for computer technology (materially nonlinear analysis (MNA), linear elastic bifurcation analysis (LBA))
- Computer technology using FE analysis consequently applied

## Plate buckling design by global numerical GMNIA analysis

- Excellent background knowledge for shell stability required (e.g. correct application of imperfections (pre-forming) is complex)
- Considerable requirements for computer technology
- Difficult application in real design situations

# Example: Plate Buckling Design by Global Numerical MNA/LBA Analysis acc. to [3]



## Technical data

Liquid:  $\gamma = 10 \text{ kN/m}^3$

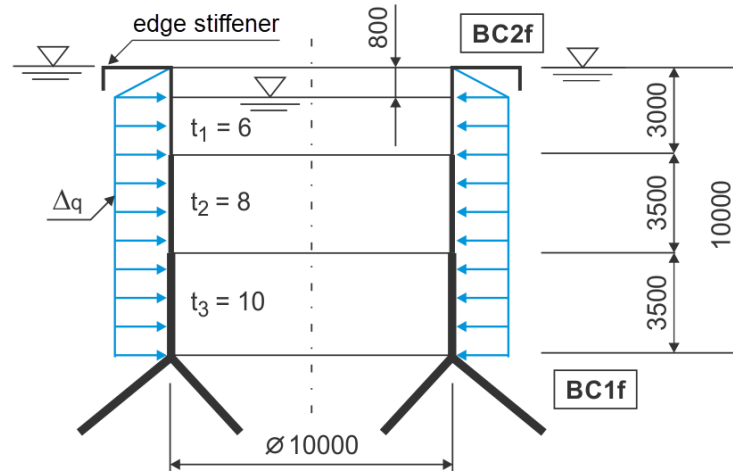
Material: S 235

Manufacturer quality: class A

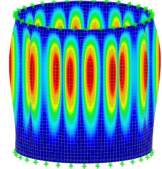
**Load** (1.0 x differential pressure)

$\Delta q_d = 8.0 \text{ kN/m}^2$

## System







## Analysis

Elastic critical buckling resistance ratio

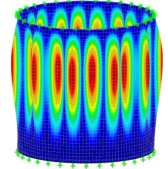
$$r_{Rcr} = 1.507 \text{ (FE eigenvalue analysis (LBA) in RFEM)}$$

Plastic reference resistance ratio ([2], Eq. 8.24)

$$r_{Rpl} = t \cdot f_{yk} / \sqrt{n_{x,Ed}^2 - n_{x,Ed}n_{\theta,Ed} + n_{\theta,Ed}^2 + 3n_{x\theta,Ed}^2}$$

The lowest value of plastic resistance ratio so calculated should be taken as the estimate of the plastic reference resistance ratio  $r_{Rpl}$ .

NOTE: A safe estimate of  $r_{Rpl}$  can usually be obtained by applying expression (8.24) in turn at the three points in the shell where each of the three buckling-relevant membrane stress resultants attains its highest value, and using the lowest of these three estimates as the relevant value for  $r_{Rpl}$ . [2]



## Analysis

$r_{Rpl} = 35.6$  (materially non-linear analysis (MNA in RFEM))

Overall relative slenderness ([2], Eq. 8.25)

$$\bar{\lambda}_{ov} = \sqrt{r_{Rpl}/r_{Rcr}}$$

$$\bar{\lambda}_{ov} = \sqrt{35.6/1.507}$$

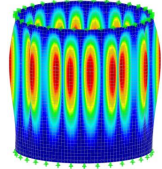
$$\bar{\lambda}_{ov} = 4.86$$

Circumferential elastic imperfection reduction factor ([2], Tab. D.5)

$$\alpha_{ov} = \alpha_{\theta} = 0.75$$

Plastic range factor ([2], D.26)

$$\beta = 0.60$$



## Analysis

Plastic limit relative slenderness ([2], Eq. 8.16)

$$\bar{\lambda}_p = \sqrt{\alpha/(1 - \beta)}$$

$$\bar{\lambda}_p = \sqrt{0.75/0.40}$$

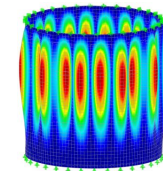
$$\bar{\lambda}_p = 1.37 \ll 4.86 \rightarrow \text{pure elastic plate buckling}$$

Buckling reduction factor ([2], Eq. 8.15)

$$\chi_{ov} = \frac{\alpha}{\bar{\lambda}^2}$$

$$\chi_{ov} = 0.75/4.86^2$$

$$\chi_{ov} = 0.0318$$



## Analysis

Characteristic buckling resistance ratio ([2], Eq. 8.26)

$$r_{Rk} = \chi_{ov} \cdot r_{Rpl}$$

$$r_{Rk} = 0.0318 \cdot 35.6$$

$$r_{Rk} = 1.132$$

Design buckling resistance ratio ([2], Eq. 8.27)

$$r_{Rd} = r_{Rk} / \gamma_{M1}$$

$$r_{Rd} = 1.132 / 1.1$$

$$r_{Rd} = 1.03 > 1 \rightarrow \text{design fulfilled}$$

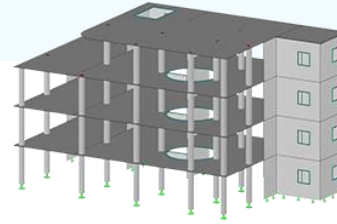
[→ Another example available in Knowledge Base](#)



# Bibliography

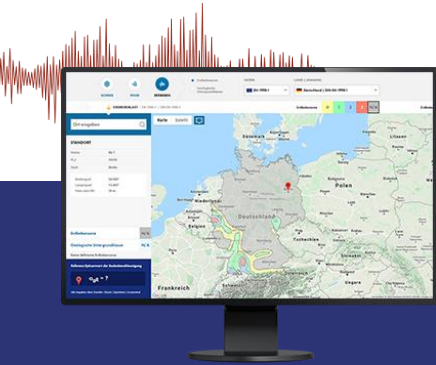
- [1] Eurocode 3: Design of steel structures – Part 1-5: General rules – Plated structural elements; EN 1993-1-5:2006 (E)
- [2] Eurocode 3: Design of steel structures – Part 1-6: Strength and stability of shell structures, EN 1993-1-6:2007 (E)
- [3] Schmidt H.: Beulsicherheitsnachweise für Schalen nach dem neuen Eurocode EN 1993-1-6 – Ein Überblick mit Beispielen aus der Anwendungspraxis, Referat beim 27. Stahlbau-Seminar in Neu-Ulm und Wien, 2005

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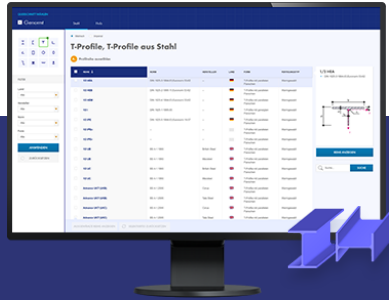
## Geo-Zone Tool

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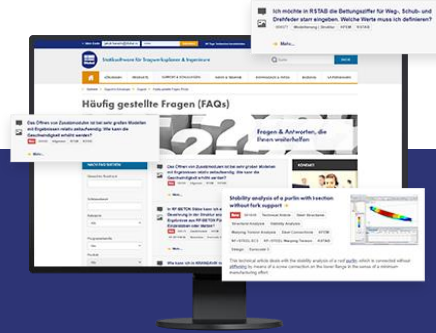
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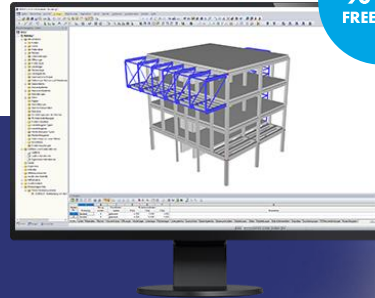
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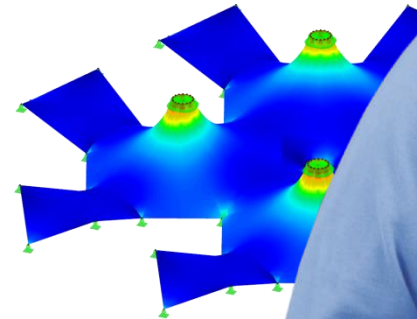
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